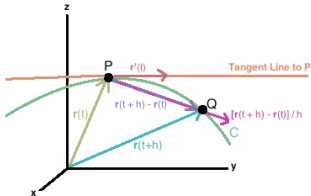


1. Goals



By the end of this unit, students will:

- understand the concepts and techniques in vectors, complex numbers, functions and graph sketching
- apply reasoning skills and solve problems in vectors, complex numbers, functions and graph sketching
- communicate their arguments and strategies when solving problems
- construct proofs of results
- interpret mathematical information and ascertain the reasonableness of their solutions to problems.

This week:

- differentiate and integrate a vector function with respect to time
- determine equations of motion of a particle travelling in a straight line with both constant and variable acceleration

2. Theoretical Components

Refer to PDF on G/Drive for notes and examples on Vector Calculus.

The following videos will help explain key points (via examples) and will make it easy to understand:

Derivative of a vector valued function:

<https://goo.gl/cjiPJ8>

<https://goo.gl/qtxyyP>

Position, Velocity & Acceleration:

<https://goo.gl/Qzf2yE>

<https://goo.gl/iFKjMh>

<https://goo.gl/OdmSV4>

Extension: Dare!!!

Vector Calculus in a nutshell: <https://bit.ly/2WKI9iH>

Calculus of Motion: <https://bit.ly/2YBHMrv>

3. Practical Components

Attempt the questions in the PDF (G/Drive/WK14 folder)

Prepare well for the Open Book In-Class Exercise (scheduled for WK16 Friday, L4)

4. Investigation

A: Describe the parametric curve represented by the equations $x = a \cos t$ $y = a \sin t$ $z = ct$
5 marks

B: Graphs of vector valued functions can range from continuous and smooth to discontinuous and wildly erratic. A curve $r(t)$ is smoothly parametrized by $r(t)$, or that $r(t)$ is a smooth function of t if $r'(t)$ is continuous and $r'(t) \neq 0$ for any allowable value of t . Geometrically, this means that a smoothly parametrized curve can have no abrupt changes in direction as the parameter increases. Determine whether the following vector valued functions are smooth.

a) $r(t) = a \cos t \mathbf{i} + a \sin t \mathbf{j} + ct \mathbf{k}; \quad a \text{ \& } c > 0$

b) $r(t) = t^2 \mathbf{i} + t^3 \mathbf{j}$

6 marks

5.QFO

Quiz/Forum/Other

Race cars with constant speed around curve: <https://goo.gl/60dZdT>