## Goals

This fortnight we are going to:

- Reviewing rate of change, gradient and key features of graphs
- Review index laws and exponential functions
- Define logarithms definition and learn their algebraic properties
- Sketch logarithmic functions
- Solving indicial and logarithmic equations using any base
- Investigate Euler's number
- Use natural logarithms to the base $e$ (Learn notation used)


## Theoretical Components

## Practical Components

Make notes on the following chapters:

## Maths Quest 12 Mathematical Methods

- 3A - The index laws
- 3B - Logarithm laws
- 3C - Exponential equations
- 3D - Logarithmic equations using any base
- 3E - Exponential equations (base $e$ )
- 3 F - Equations with natural (base $e$ ) logarithms


## What is base $e$ ?

Learn more about Euler's number. Read through to get an insight on the number ' $e$ ':

- https://www.mathopolis.com/questions/q.ph p?id=2011\&site=1\&ref=/numbers/e-eulersnumber.html\&qs=2011 20122013
- https://betterexplained.com/articles/an-intuitive-guide-to-exponential-functions-e/


## Graphing Logarithmic Functions:

- https://www.youtube.com/watch?v=q9DhIR4 3P7A
- https://www.youtube.com/watch?v=LqyA960 YtwE


## Do the following questions:

Organise your solutions neatly in your exercise book.

Chapter 3 of Maths Quest 12 Mathematical Methods (pdf - Google Classroom)

- 3A: all
- 3B: all
- 3C: all
- 3D: 1-5 (2nd column), 8 (2nd column)
- 3E: 1-3 (2nd and 4th column), 4-6 (2nd column), 7, 8
- 3F: 1-4 (2nd column), 5-10


## Portfolio Task

See next page

Make sure you have joined the Google Classroom. If you have not, see your teacher.
Fun fact: The logarithm plays a more fundamental role in mathematics than you might realise, more often than not showing up in places you might not expect. For example, the proportion of positive integers less than $x$ that are prime can be modelled by $\frac{1}{\log (x)}$

## Week 1 and 2 Investigation

## Question 1:

a. Use the change of base rule to show that $\log _{a^{x}}\left(b^{x}\right)=\log _{a}(b)$
b. Use your knowledge from part a to simplify:
i. $\quad \log _{16} 81$
ii. $\quad \log _{\sqrt{27}} \sqrt{125}$

## Question 2:

a. Show that $\log _{a b} x=\frac{\log _{a} x}{1+\log _{a} b}$
b. Show that $\log _{2} 5=\frac{1-\log _{10} 2}{\log _{10} 2}$

