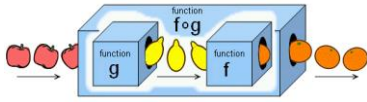


## Goals



Source: <https://goo.gl/tz6S4i>

By the end of this unit, students will:

- understand the concepts and techniques in vectors, complex numbers, functions and graph sketching
- apply reasoning skills and solve problems in vectors, complex numbers, functions and graph sketching
- communicate their arguments and strategies when solving problems
- construct proofs of results
- interpret mathematical information and ascertain the reasonableness of their solutions to problems.

### This week: Functions and sketching graphs

- determine when the composition of two functions is defined
- find the composition of two functions
- determine if a function is one-to-one
- consider inverses of a one-to-one functions
- examine the reflection property of the graph of a function and the graph of its inverse.

## Theoretical Components

Mathspace Lessons:

Describing Functions: <https://bit.ly/3dKIcX5>

One-to-One functions: <https://bit.ly/2ZPNfh1>

Composite Functions: <https://bit.ly/2ZT2sxO>

Graphing Composite Functions:  
<https://bit.ly/2MqGYFf>

Additional readings available on Google Classroom WK05 folder.

Watch the following videos:

- Composite Functions: <https://goo.gl/FEoV7C>
- <https://goo.gl/iyQ9df>
- Inverse Functions: <https://goo.gl/nLcmkb>  
<https://goo.gl/WIFLM5>

## Practical Components

Check Google Classroom WK05 folder:

Ex: Composite Functions Mathspace Questions

Ex: One-to-One Mathspace Questions

Ex: Graphing Comp Functions Mathspace Questions

Attempt at least 10 questions from each of the listed exercises.

## Investigation

See the next page.

20 marks – see rubric.

Q/F/O  
Quiz/Forum/Other

Mathspace Quiz: to be completed by 7<sup>th</sup> March.

## Investigation

**Part A:**

Let  $G(x, y, z) = \begin{bmatrix} x + 2yz \\ x^2 + y \\ z^2 + x \end{bmatrix}$  and  $F(u, v, w) = u^2 + v + wi$ .

Find  $F \circ G(1, 1, -1)$ . State your answer in polar form.

**Part B:**

You are expected to use your understanding of derivatives (SMM) and composite functions (SM) to discuss:

$$\frac{d}{dx}(3x + 7)^5 = 15(3x + 7)^4$$

Key words: derivatives, composite functions.

**Part C:**

Consider the function  $f(x) = \frac{x+1}{x-1}$ ;  $x \neq \pm 1$ . Find  $f \circ f \circ f(x)$  and  $f \circ f \circ f \circ f(x)$ .

Research about the result and provide a short description.