Week 9/10 4 Term 2023



**Learning Brief** SM<sub>2</sub>

# Goals

By the end of this unit, students:

- understand the concepts and techniques in trigonometry, real and complex numbers, and matrices
- apply reasoning skills and solve problems in trigonometry, real and complex numbers, and matrices
  - communicate their arguments and strategies when solving problems

Engage | Inspire | Achieve

- construct proofs of results
- interpret mathematical information and ascertain the reasonableness of their solutions to problems This week:
- **Complex Numbers:**
- define the imaginary number i as a root of the equation  $x^2 = -1$
- use complex numbers in the form a + bi where a and b are the real and imaginary parts
- determine and use complex conjugates
- perform complex-number arithmetic: addition, subtraction, multiplication and division.

## Theoretical Components

#### Read through examples and make notes.

What are Complex Numbers: https://bit.ly/3c4qCKM

Addition & Subtraction of Complex Numbers: https://bit.ly/3iE8aeF

Multiplication of Complex Numbers: https://bit.ly/33zS2EB

Powers of i:

https://bit.ly/3hzK7MF

**Complex Conjugates:** https://bit.ly/32CiTkd **Complex Numbers & Four Operations:** https://bit.ly/3hDFXDx



This Mandelbrot set shows how fractal geometry creates order out of what seem like irregular patterns. Points that are not in the Mandelbrot set are colour based on how quickly they diverge. Benoit Mandelbrot (b 1924), left, was the first person to study and name fractal geometry.

### **Practical** Components

Check Google Drive 2023S2/WK10 folder:

(Answer all questions)

## Investigation

The sum of two numbers, x and y, is 10, and A: their product is 40. Find the numbers x and y.

This investigation is based on a problem that was posed by Cardon in 1545 that saw the need to introduce complex numbers in the 16<sup>th</sup> century.

Β. There is a complex number m with the imaginary part 164 and a positive integer n such that

$$\frac{m}{m+n} = 4i$$

Find n.

20 marks



This will help you visualise Mandlebrot Set Process:

https://www.desmos.com/calculator/uscgu3skam

