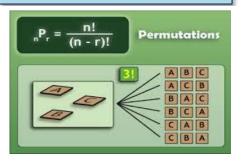


Learning Brief SMM1: Counting and Probability

Goals



By the end of this week, you should be able to:

- Use <sup>n</sup>P<sub>r</sub> to count number of possible arrangements (permutations)
- Compute number of ways of arranging n objects which include
  p identical objects of one type, q identical objects of another
  type, r identical objects of yet another type...
- Compute number of arrangements when n objects divided into m groups
- Compute number of arrangements when distinguishable objects are arranged in a circle

## Theoretical Components

#### STEP 1

You will require Chapter 12 of Maths Quest 11 Mathematical Methods (pdf - Google Classroom)

- ✓ Read through Section 12B on <sup>n</sup>P<sub>r</sub> Permutations. Study examples 5 - 7
- ✓ Read through Section 12D on. Study and make notes on Examples 11 -14.
- ✓ Read through Section 12E on Permutations with restrictions. Study examples 15 - 18.
- ✓ Read through Section 12F on Arrangement in a circle. Study examples 19 - 21.

Make your notes on the following key concepts:

- Permutations with restrictions, repetitions
- Arrangements in a circle

| ABCD | ABDC | ACBD | <b>ACDB</b> | <b>ADBC</b> | <b>ADCB</b> |
|------|------|------|-------------|-------------|-------------|
| BACD | BADC | BCAD | <b>BCDA</b> | <b>BDAC</b> | <b>BDCA</b> |
| CABD | CADB | CBAD | CBDA        | CDAB        | CDBA        |
| DABC | DACB | DBAC | DBCA        | DCAB        | <b>DCBA</b> |

#### Permutations:

http://www.tutors4you.com/circularpermutations.htm

### Practical Components

#### STEP 2

You will require Chapter 12 of Maths Quest 11 Mathematical Methods (pdf - Google Classroom) Do the following questions. Organise your solutions neatly in your exercise book:

EX 12D: ALL even numbered questions.

EX 12E: ALL odd numbered questions.

EX 12F: ALL odd numbered questions.

Complete more of these questions if you need.

# Investigation

### STEP 3

1. Prove:

$$^{n+1} P_r = {}^{n}P_r + r_{\cdot}{}^{n}P_{r-1}$$

- 2. In how many ways can four men and four women be seated alternatively:
  - a. in a row,
  - b. at a round table?
- 3. How many arrangements of the letters in the word TOMATO are there, if the letters O are to be separated?



Continue with these questions:

See handout (online pdf) – Set Notation Exercise 2A and 2B



Learning Brief SMM1: Counting and Probability

# Investigation

### STEP 3

1. Prove:

$$^{n+1} P_r = {}^{n}P_r + r.{}^{n}P_{r-1}$$

- 2. Four men and four women are to be seated alternatively:
  - a. in a row,
  - b. at a round table.

In how many ways can this be done?

3. How many arrangements of the letters in the word TOMATO are there, if the letters O are to be separated?

### **Extension Question:**

In how many ways can four people be accommodated in a certain hotel if there are four rooms available?